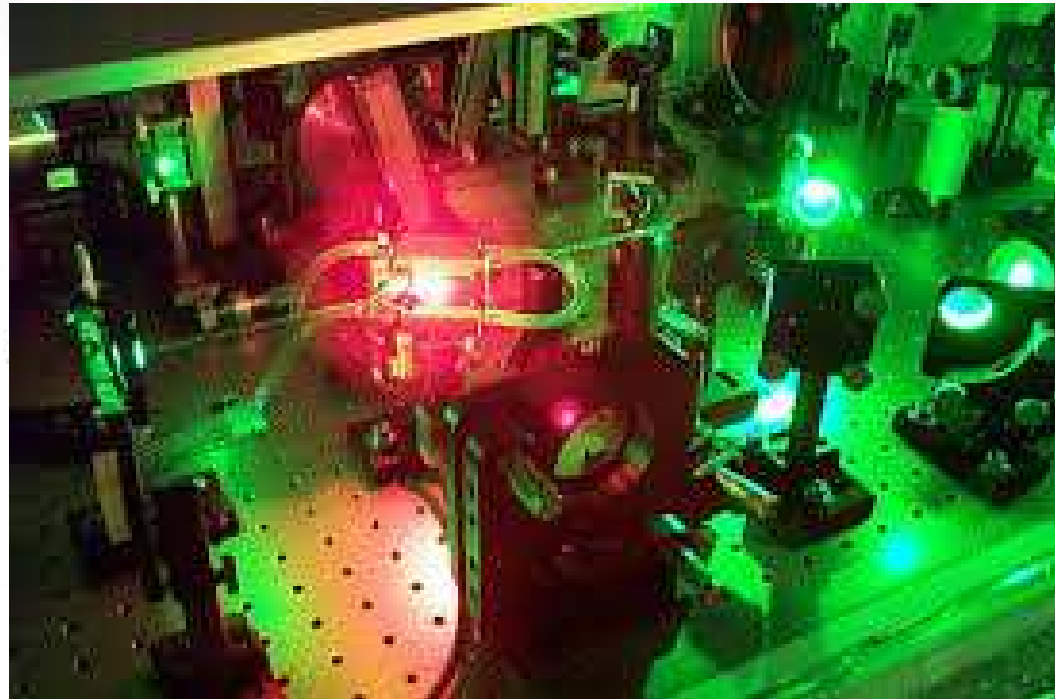
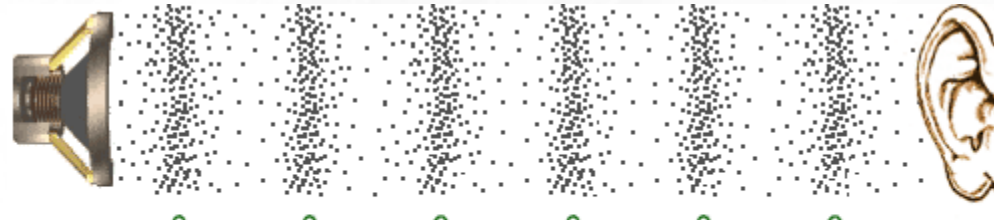


# За китарата, цигулката и ... фемтосекундните лазери



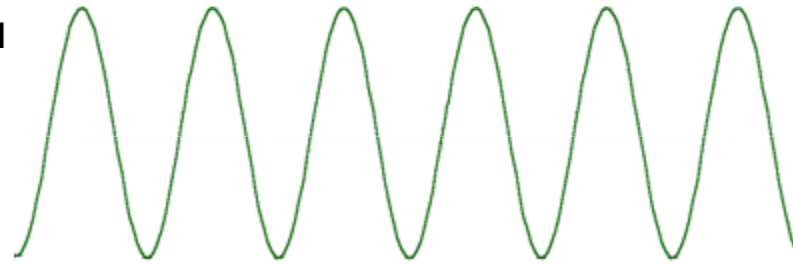
Асен Пашов,  
Физически факултет

# Какво е това звук?



Приемник

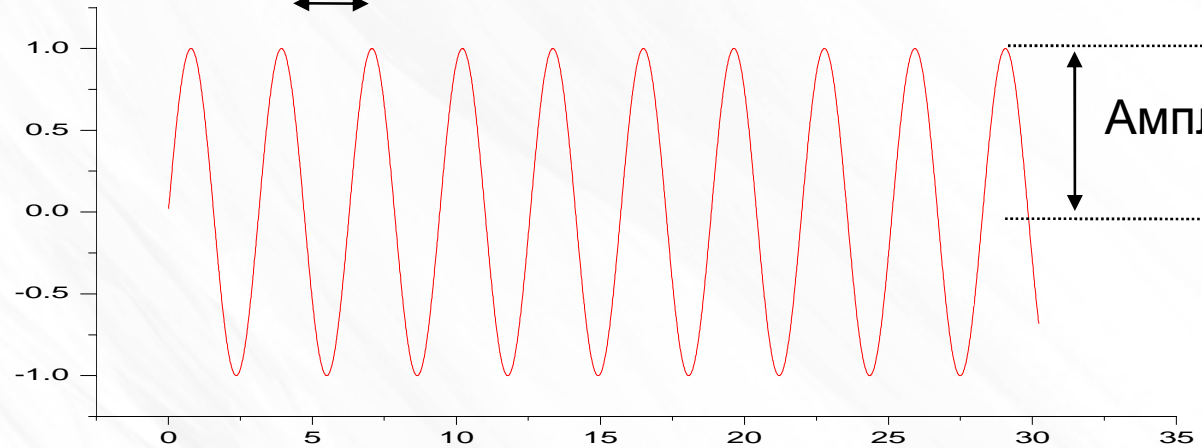
Високоговорител



Налягане на въздуха

$T$  - период  $f = 1/T$  - честота

Отместване [mm]



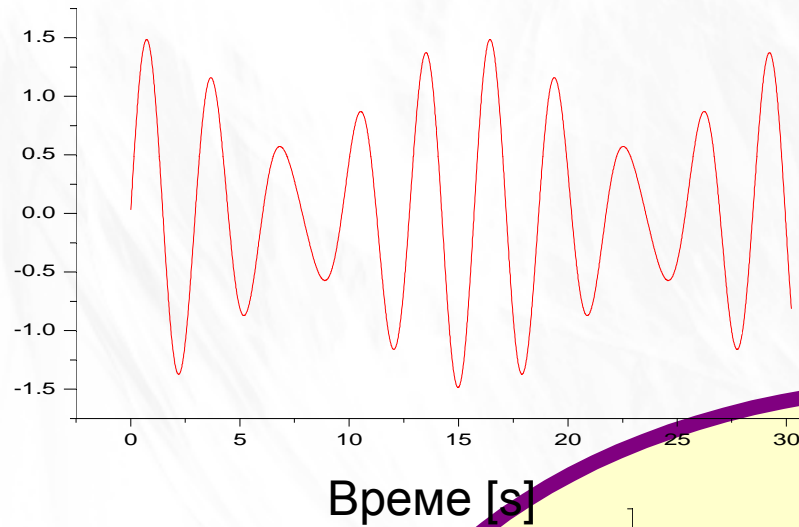
Амплитуда

Време [s]

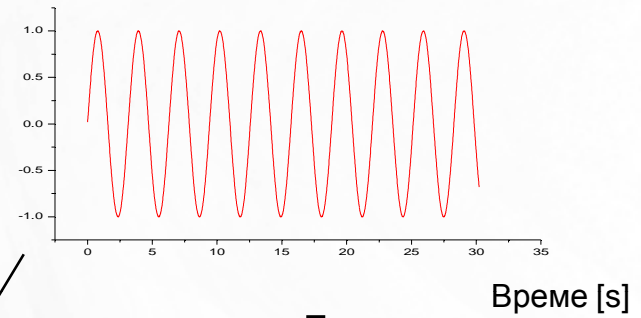


# Какво е това спектър?

Отместване [mm]

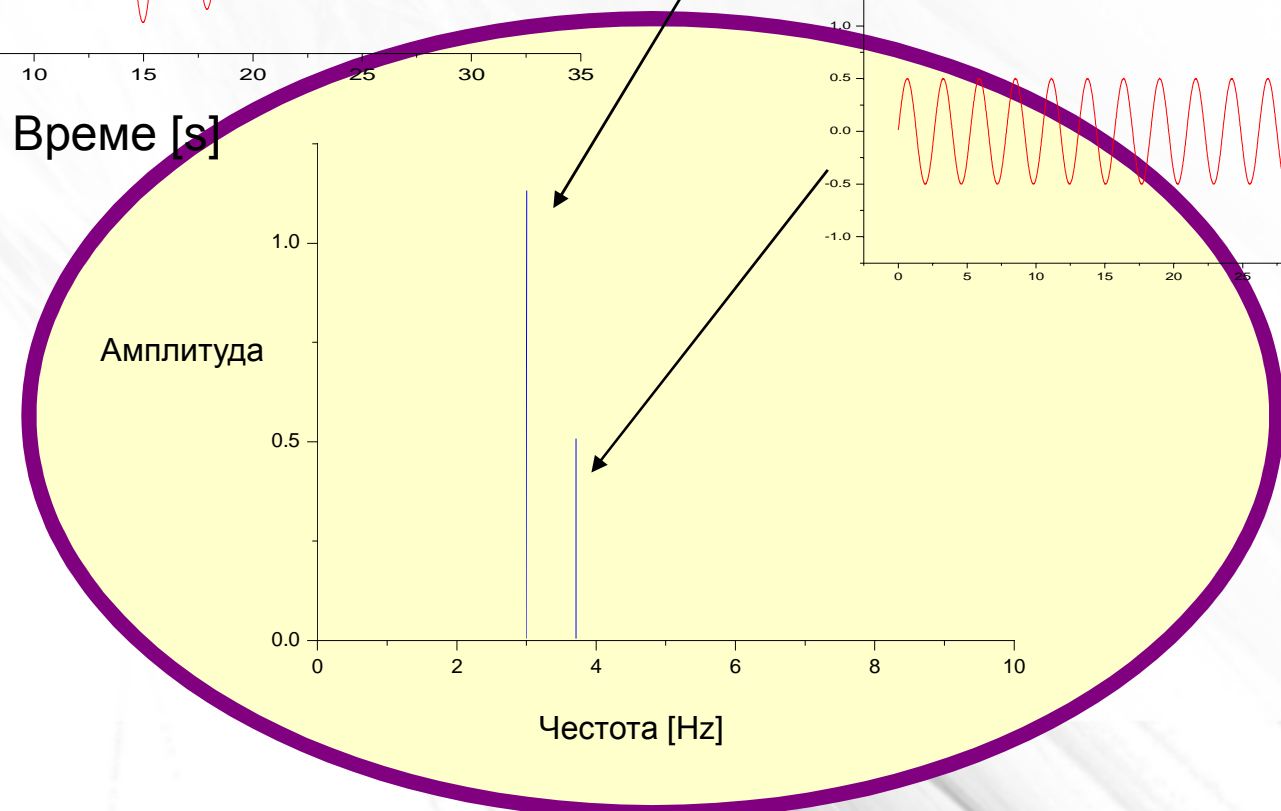
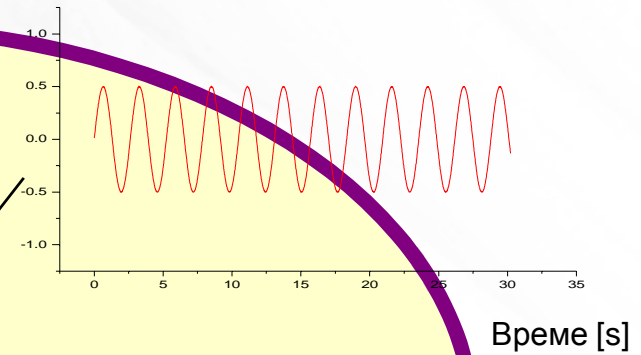


$f = 3 \text{ Hz}$



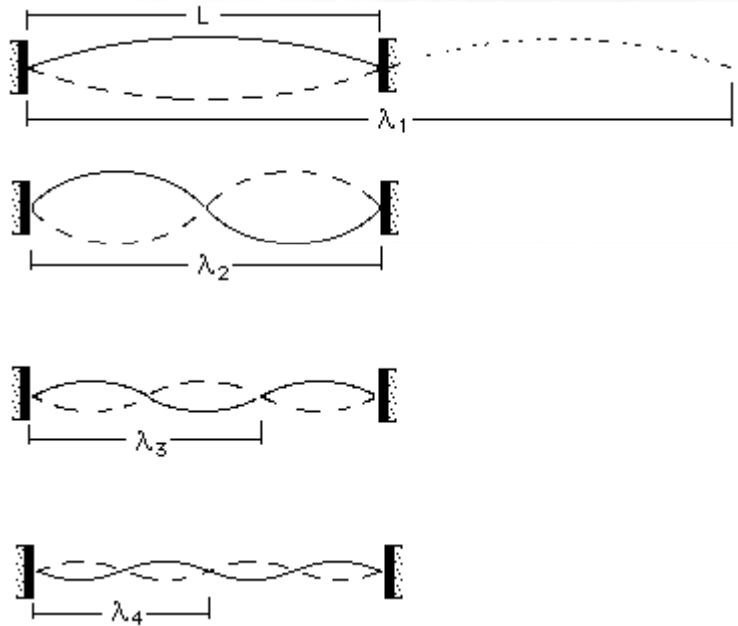
+

$f = 3.6 \text{ Hz}$



winscope

# Как може да трепти една струна?



Честота  $f$

Честота  $2f$

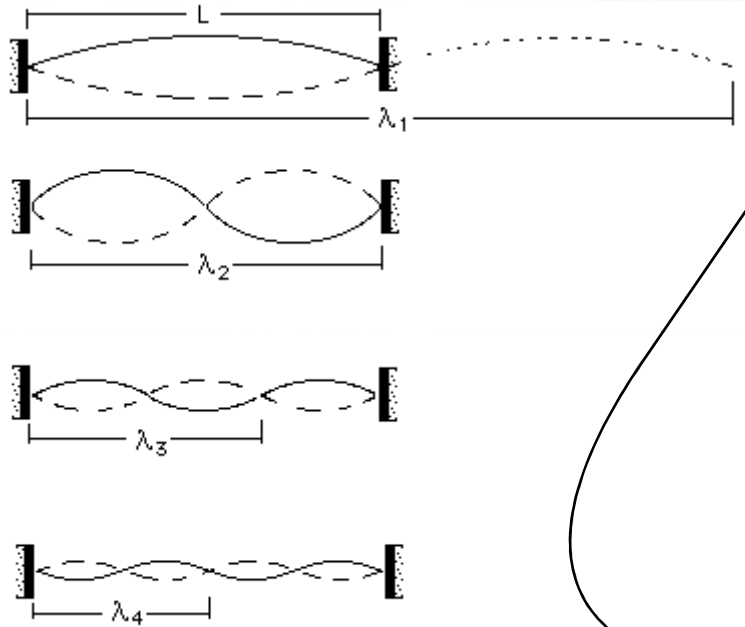
Честота  $3f$

Честота  $4f$

Мод – определен начин на трептене

Хармоници – кратни на основната честота  $f$

# Тонове и обертонове



Честота  $f$

ОСНОВЕН ТОН

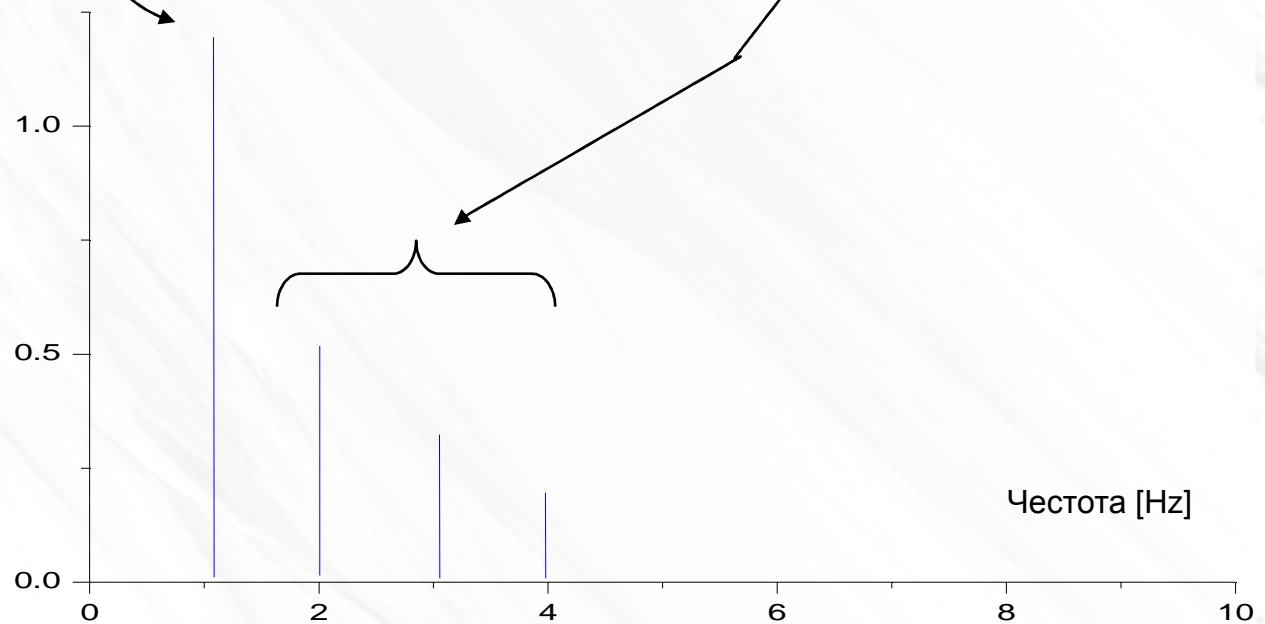
Честота  $2f$

Честота  $3f$

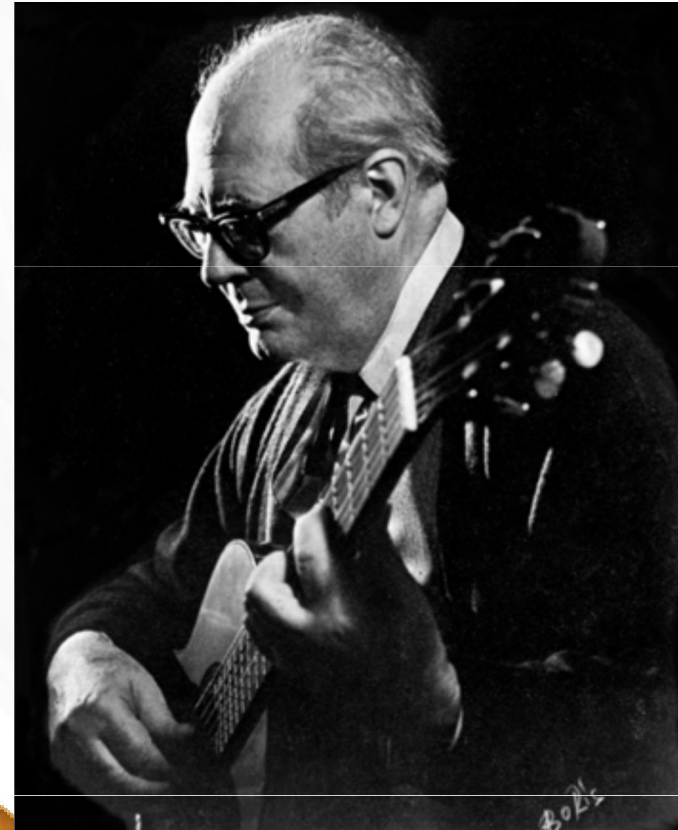
Честота  $4f$

обертонове

Спектър

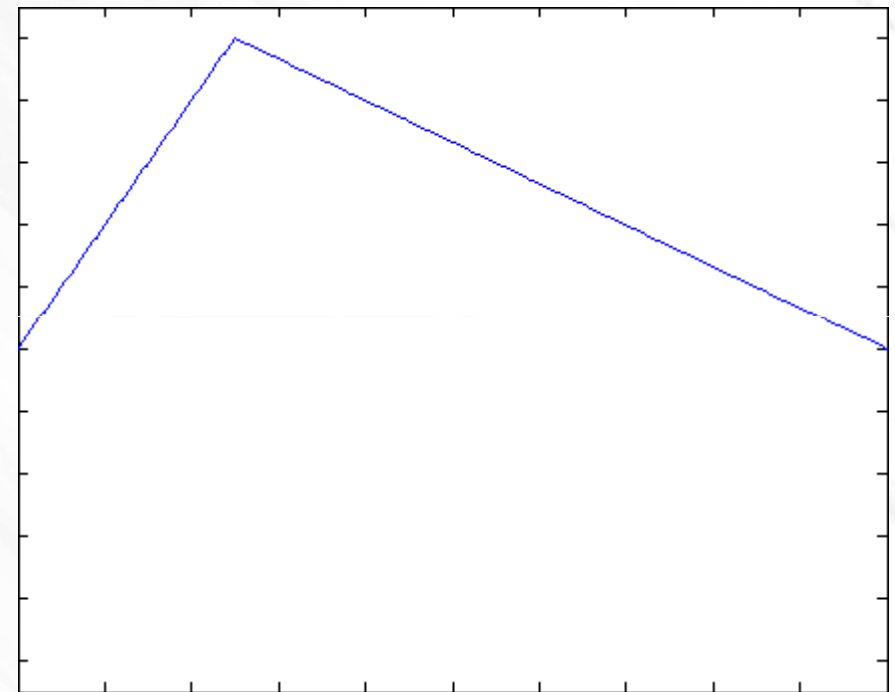
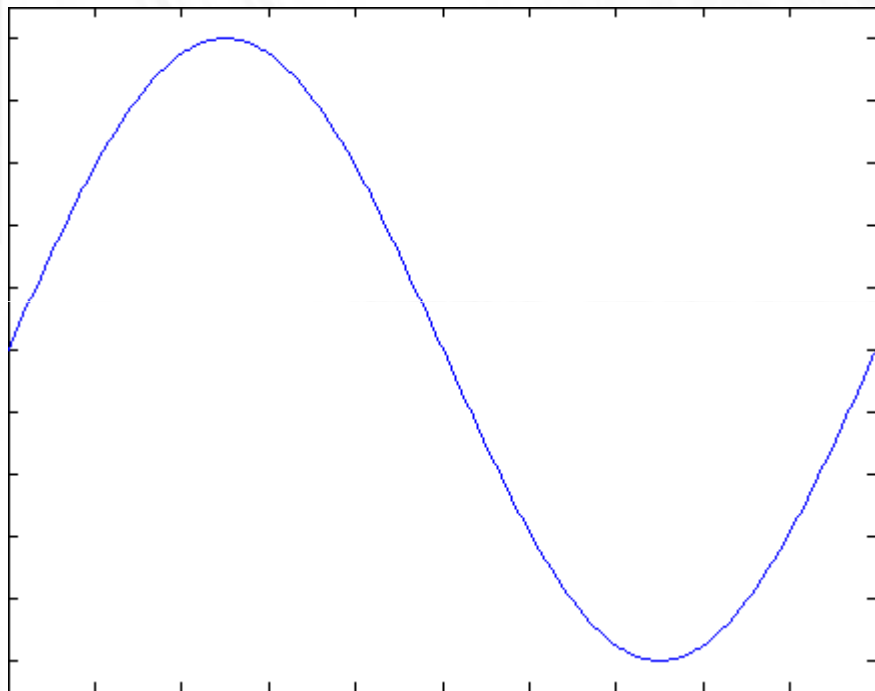
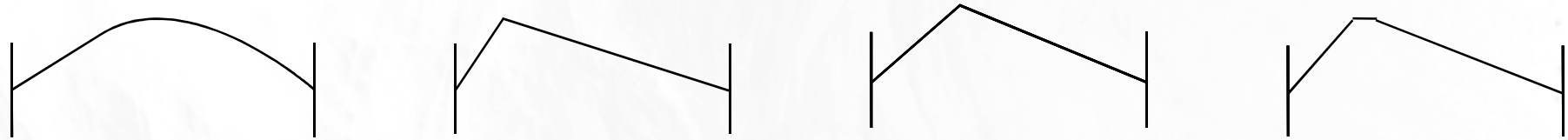


... за китарата

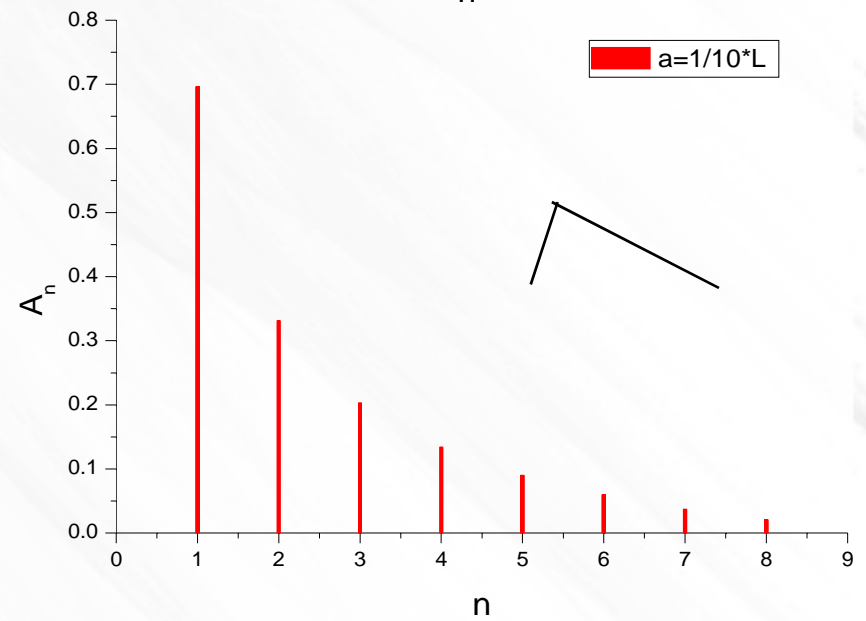
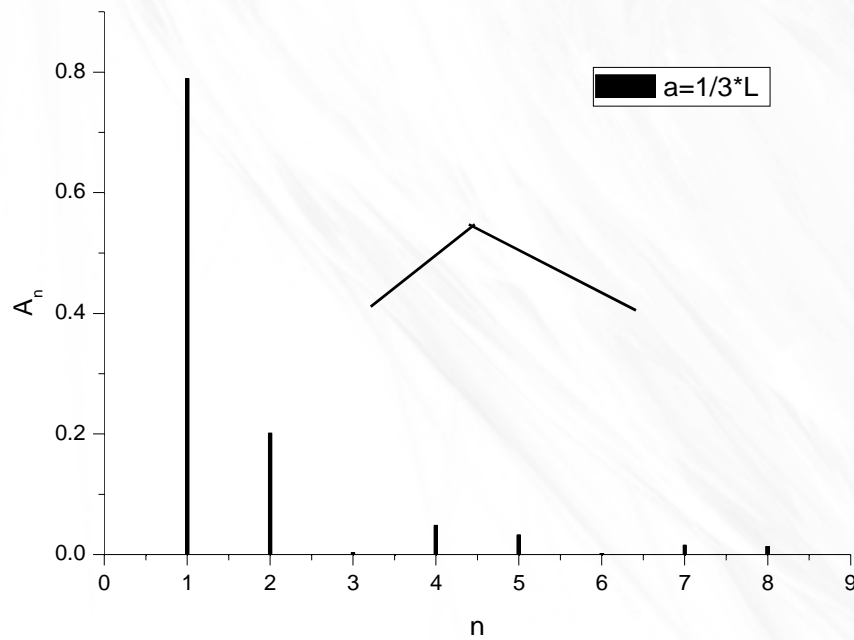
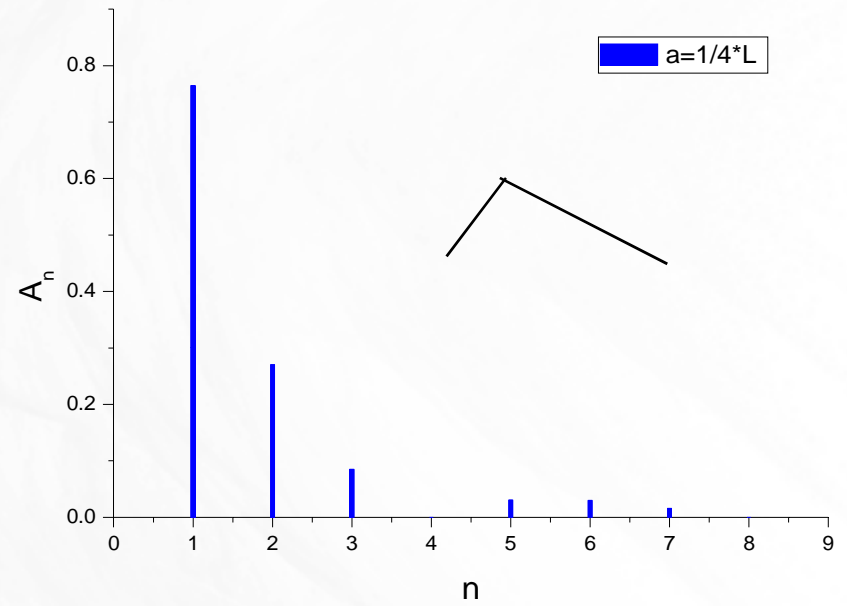
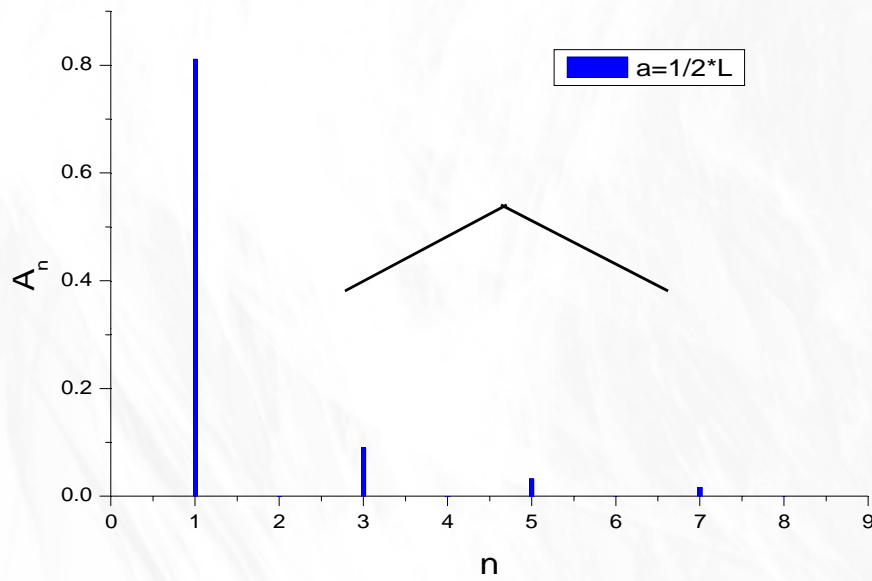


# А как наистина трепти една струна?

Начални условия:



# Отново: А как наистина трепти една струна?



winscope

# От какво зависи височината на тона?

$$f = c / 2L$$

$$f_n = n c / 2L$$

$$c = \sqrt{\frac{F}{\rho}}$$

- |                       |        |
|-----------------------|--------|
| - сила на опън        | $F$    |
| - линейна плътност    | $\rho$ |
| - дължина на струната | $L$    |

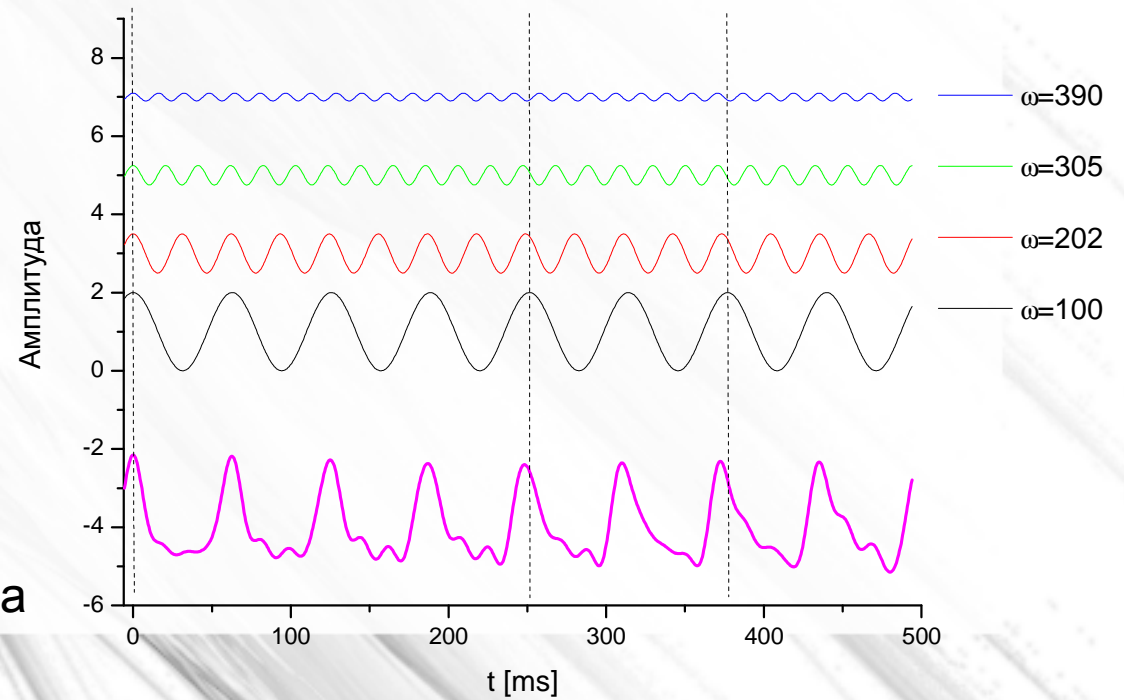
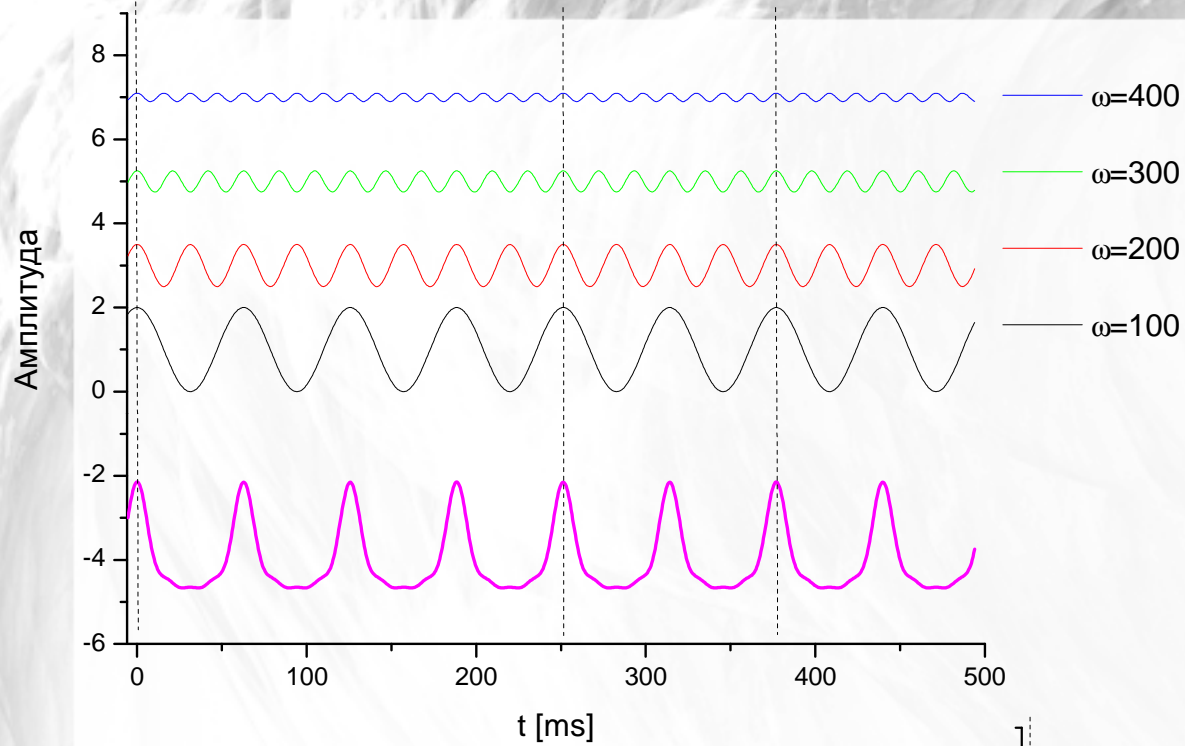
## Тънкости:

Притискането на струната променя  $F$  и  $L$

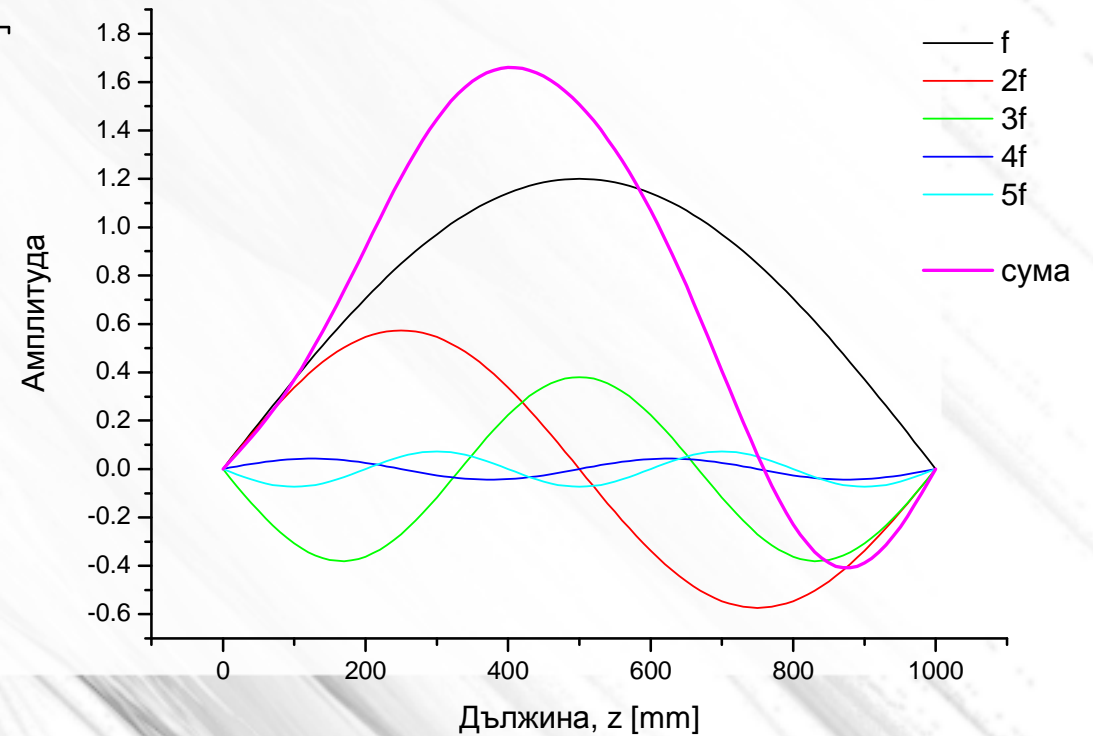
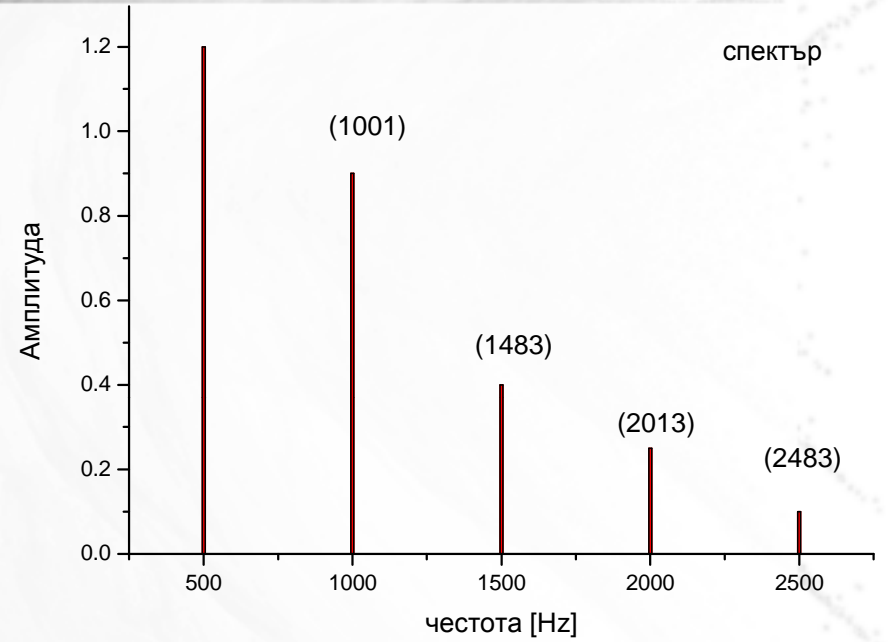
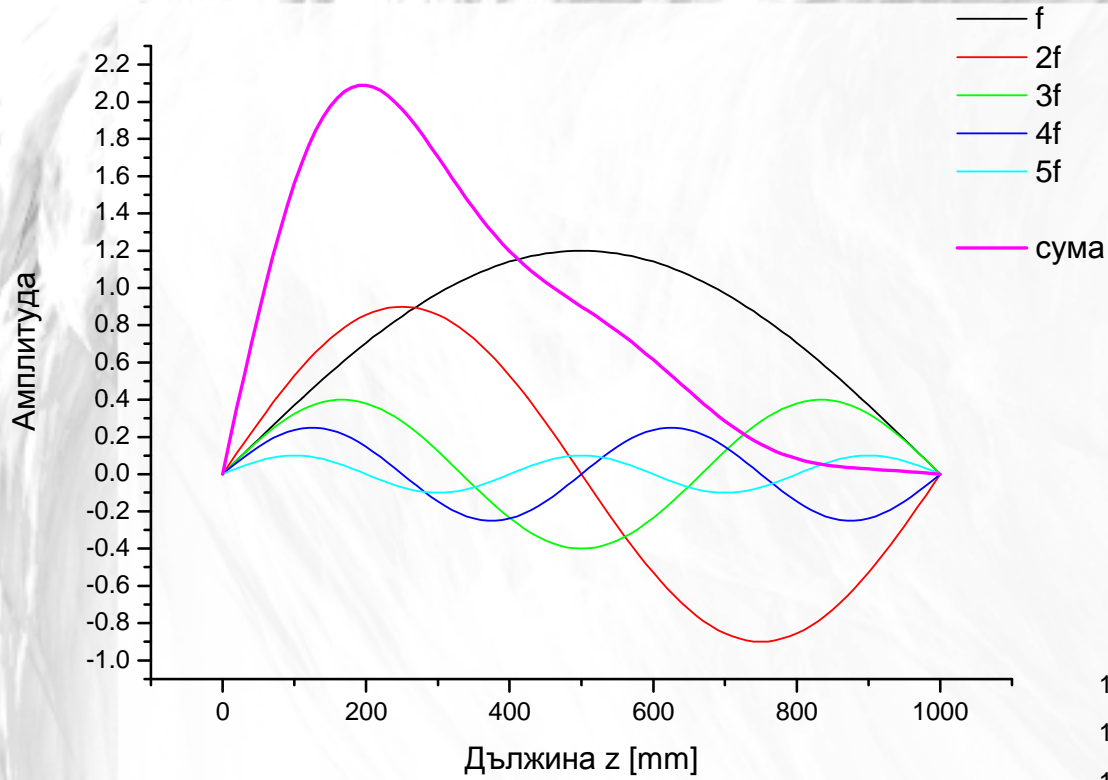
Износването и зацапването на струната променя плътността

Струната никога не е идеално тънка и еластична

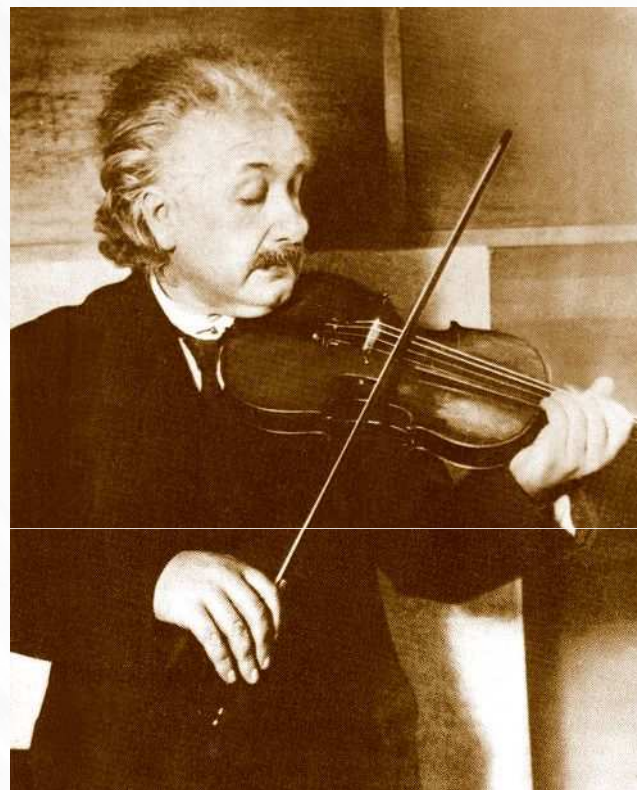
# Еднократно възбуждане, свободни трептения



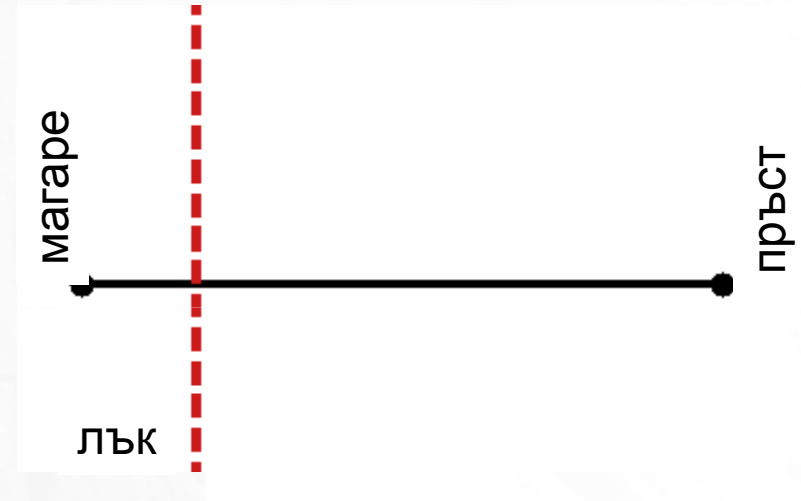
# Еднократно възбуждане, свободни трептения



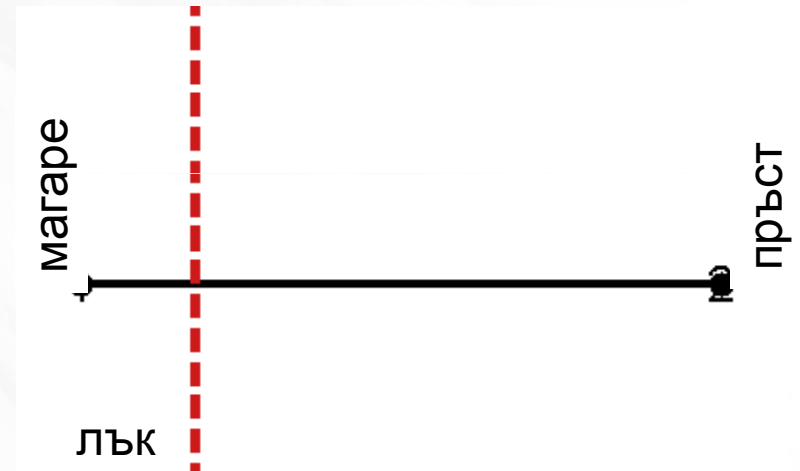
# ... за цигулката



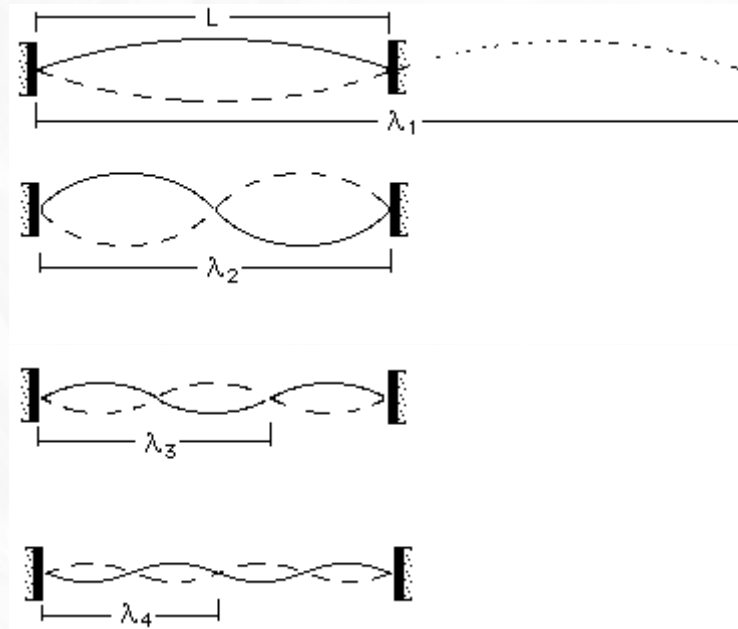
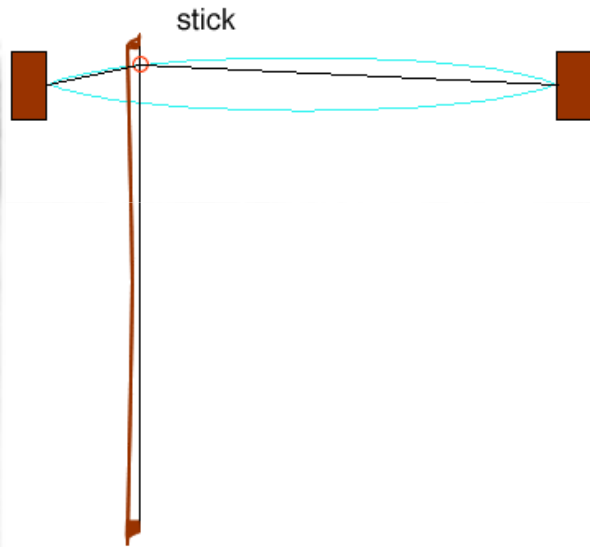
# Как трепти струната на цигулката?



Зацепване - приплъзване



# Всички модове трептят синхронно!

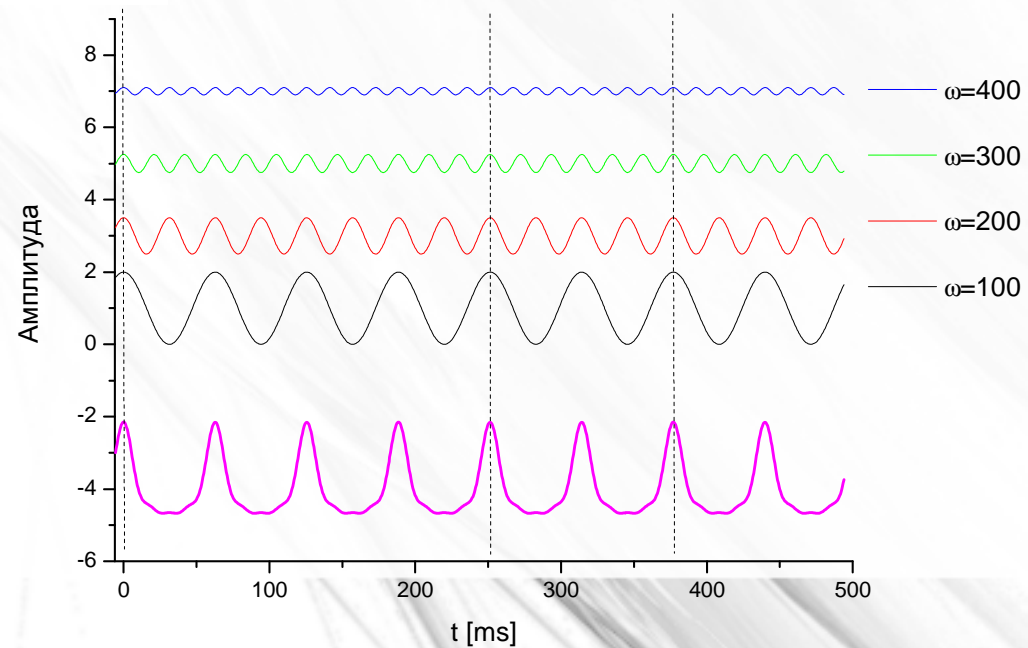


Честота  $f$

Честота  $2f$

Честота  $3f$

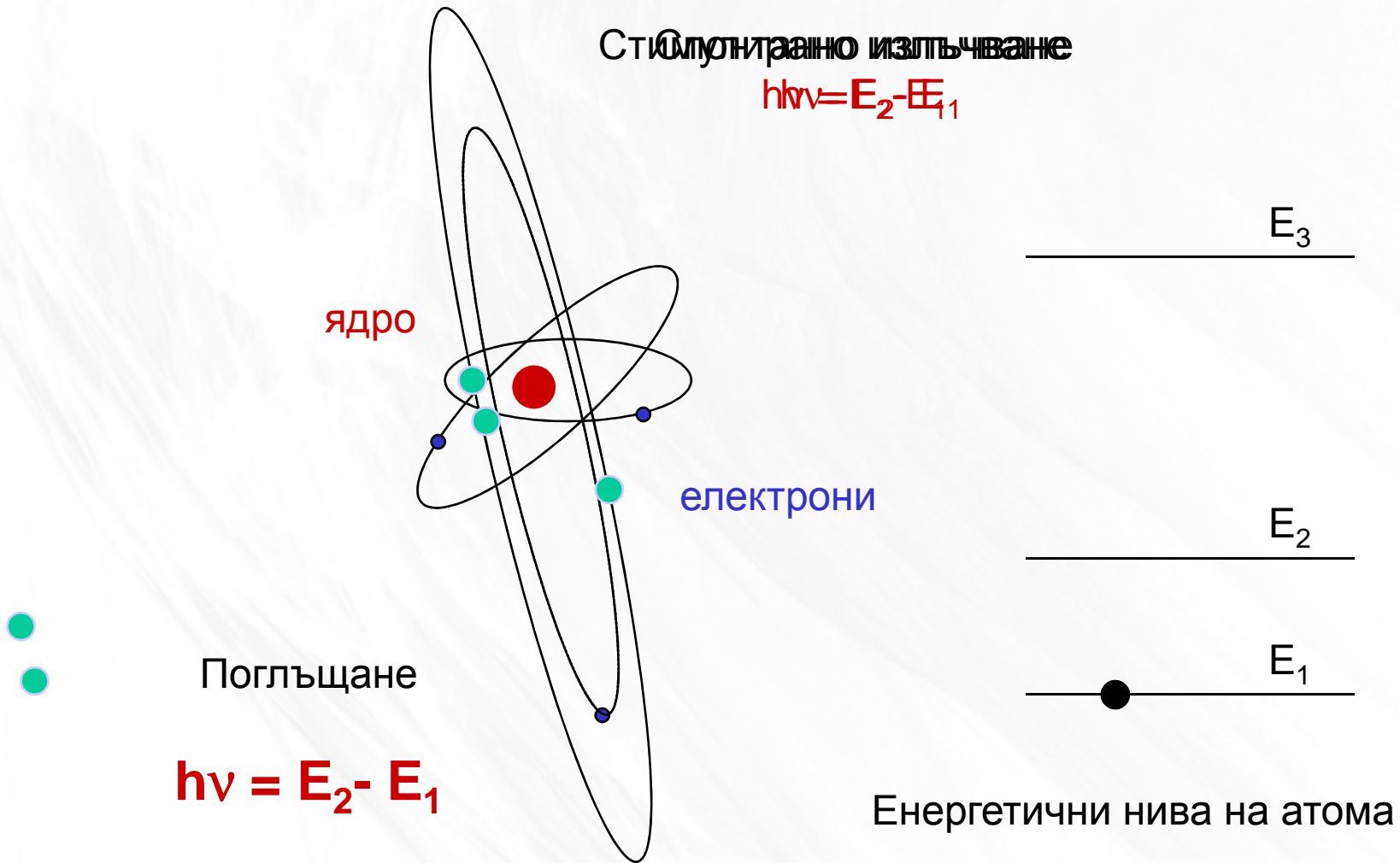
Честота  $4f$



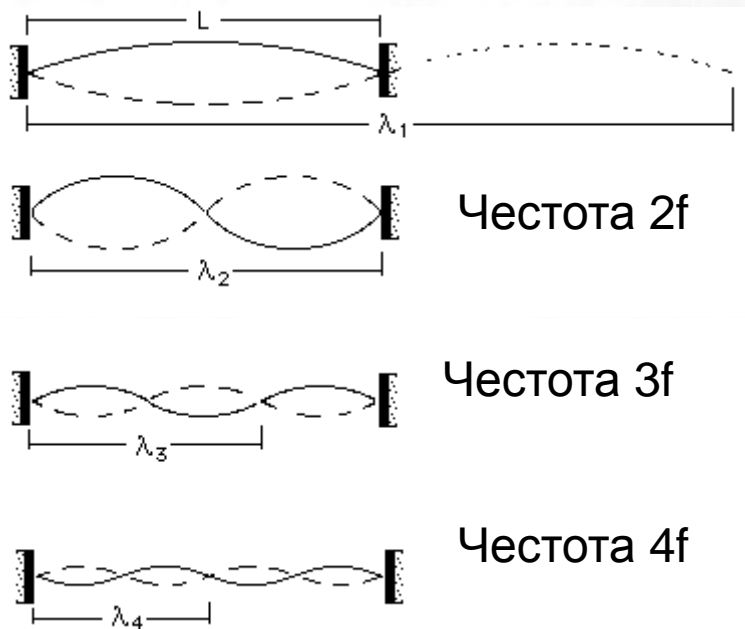
## ... за лазерите



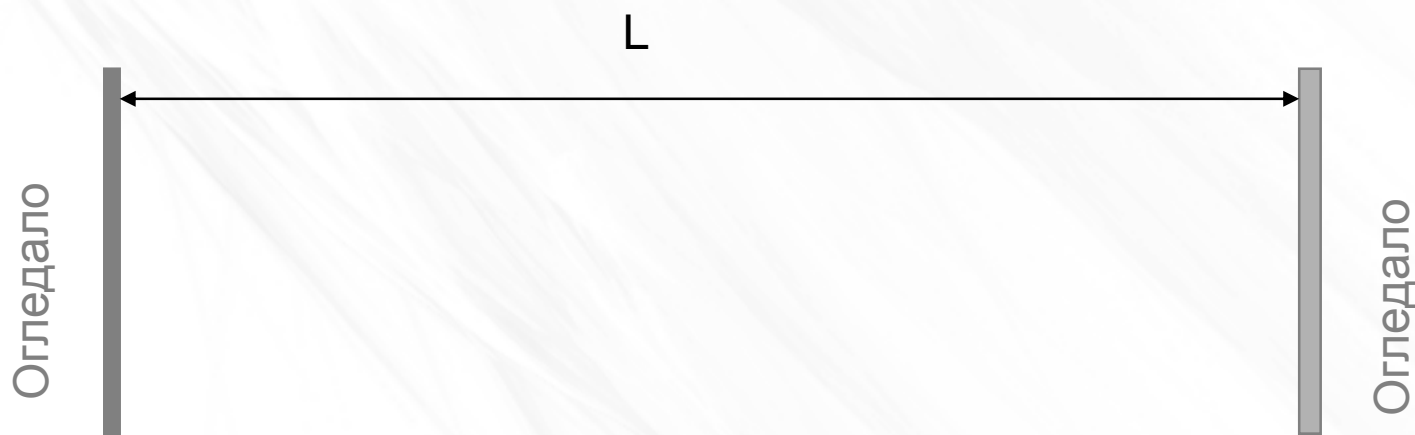
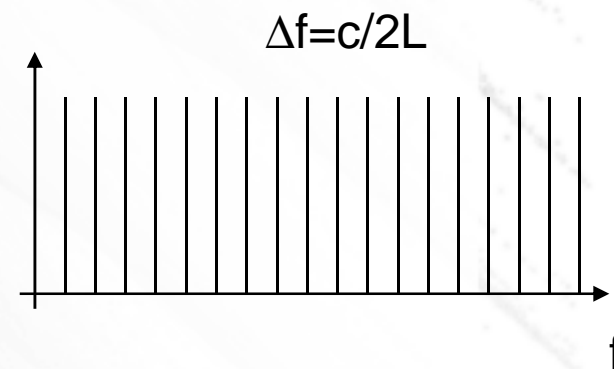
# Взаимодействие фотон – атом



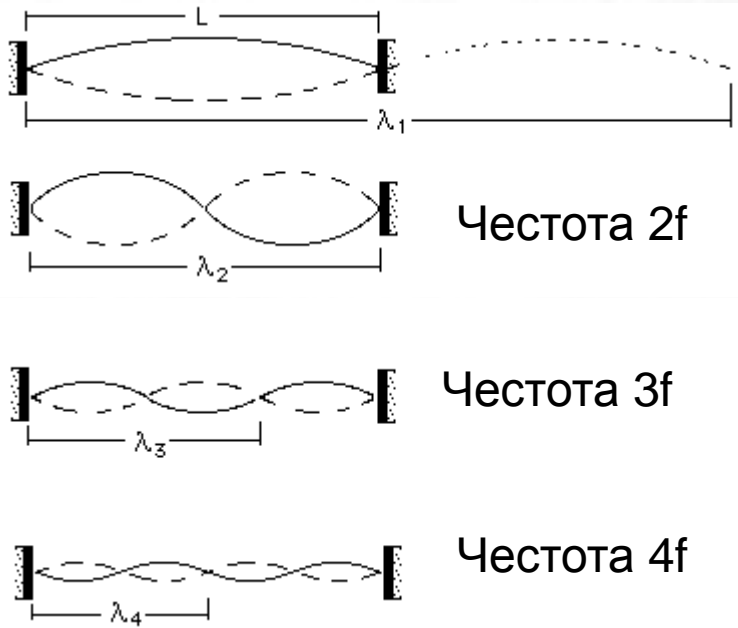




Резонатор = гранични условия!



# Цигулка и лазер



$$m = 2L/\lambda$$



$m = 1 \dots 10$

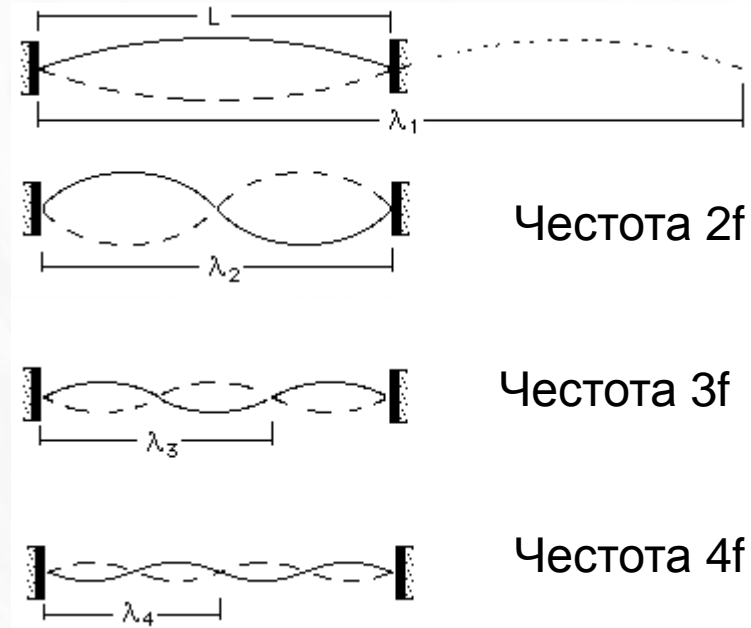
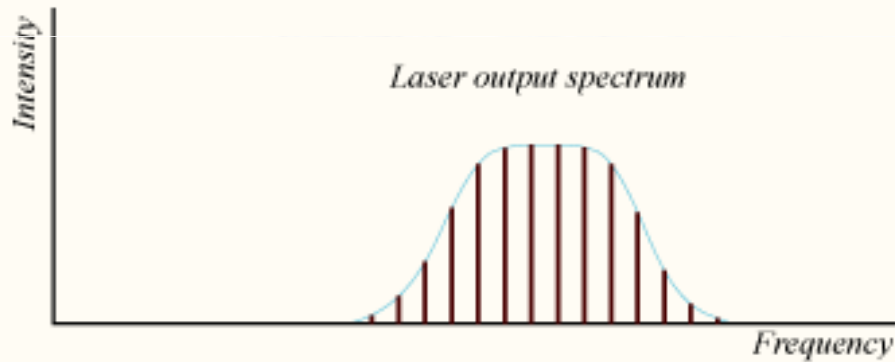
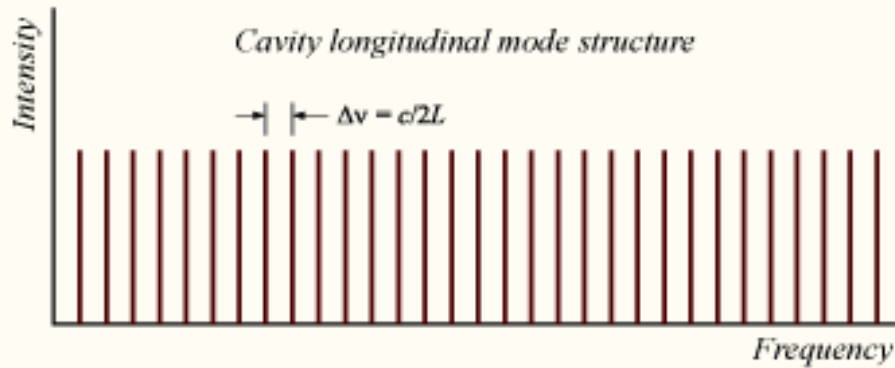
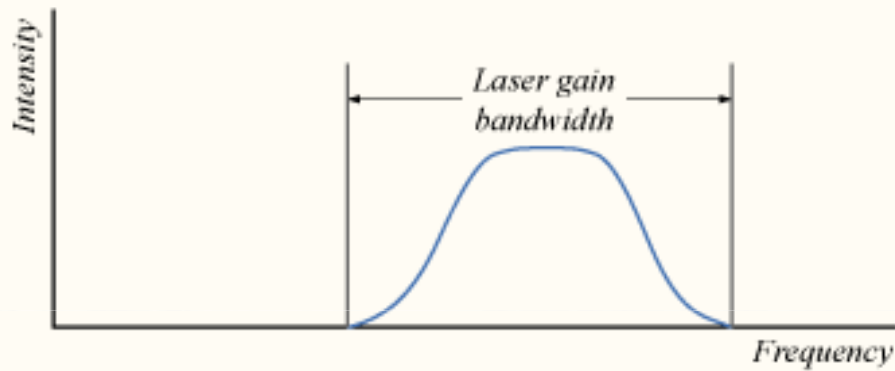
$\lambda = 65 \text{ cm} \dots 6.5 \text{ cm}$

$L = 32.5 \text{ cm}$

$m > 1\,000\,000 \dots$



# Как може да свети един лазер

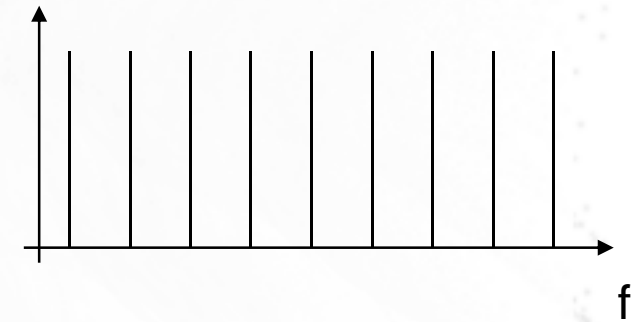


**Важно!**  
Един лазер не е задължително  
едночестотен!

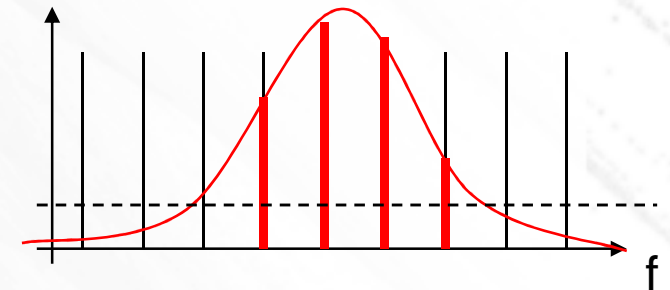
# Едночестотни лазери

Модове на резонатора

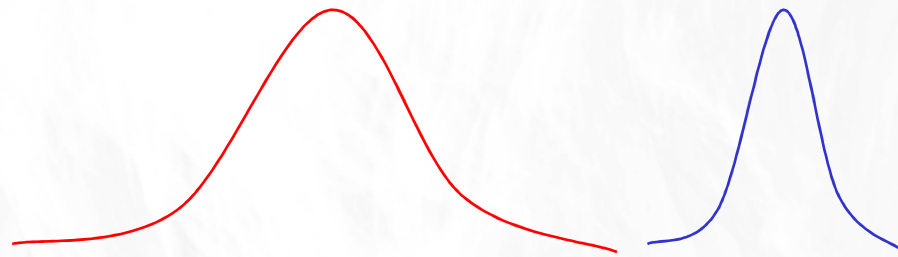
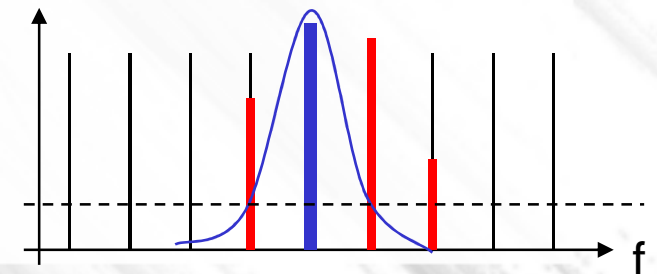
$$\Delta f = c/2L$$



Резонатор + активна среда



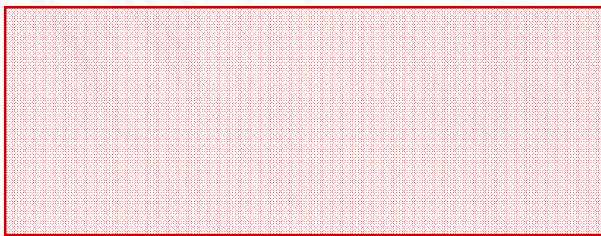
Резонатор + активна среда + селективен елемент



Селективен елемент

Активна среда

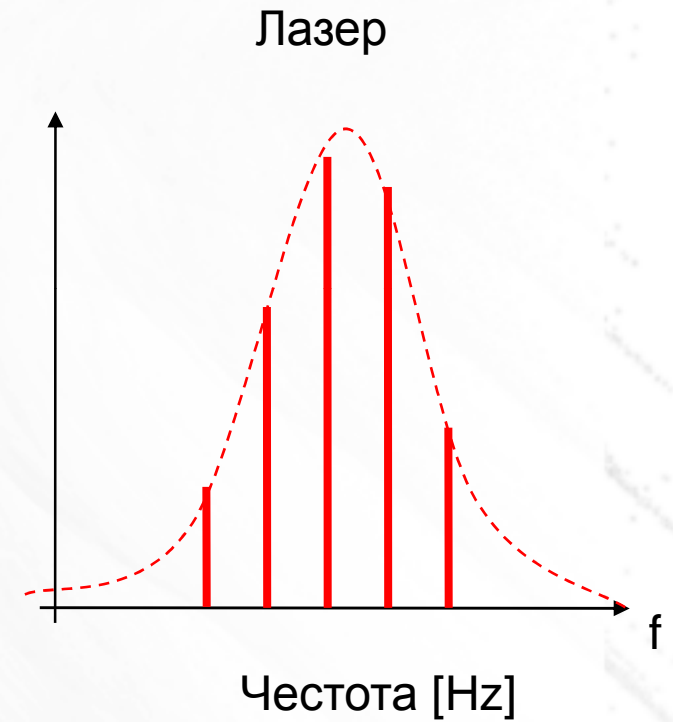
Огледало



Огледало

Генерация на един обертон!

# Лазер – китара, лазер – цигулка

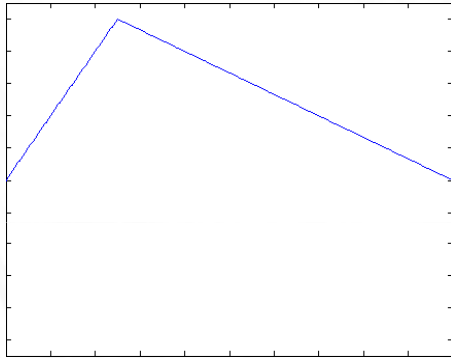


Несинхронно – китара  
Синхронно - цигулка

?

# Лазер – китара, лазер – цигулка

Различни начални условия!



Модовете са независими.

**Китара, цигулка**

Неравномерна линейна плътност  $\rho$



Различна скорост на модовете



Различна честота на модовете

**Лазер**

Дисперсия на показателя на пречупване  $n$

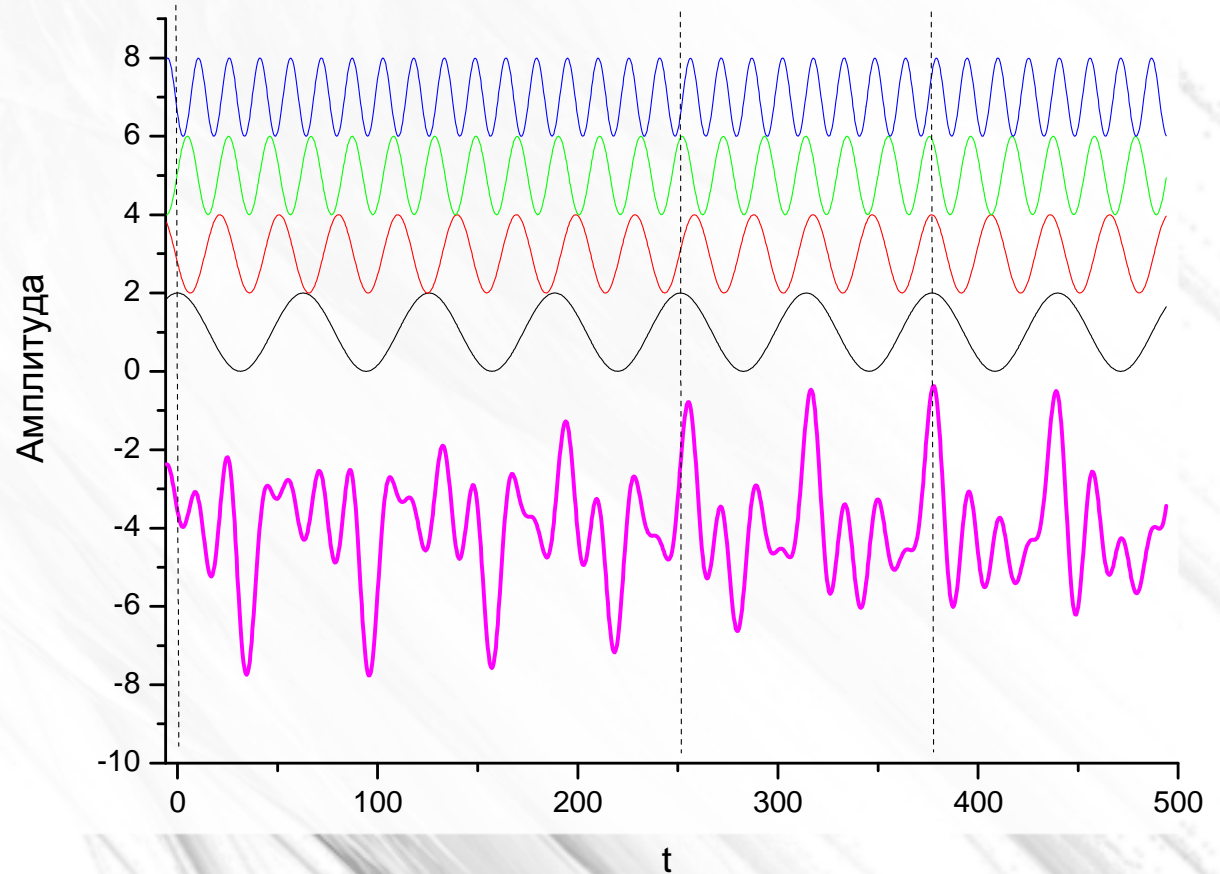
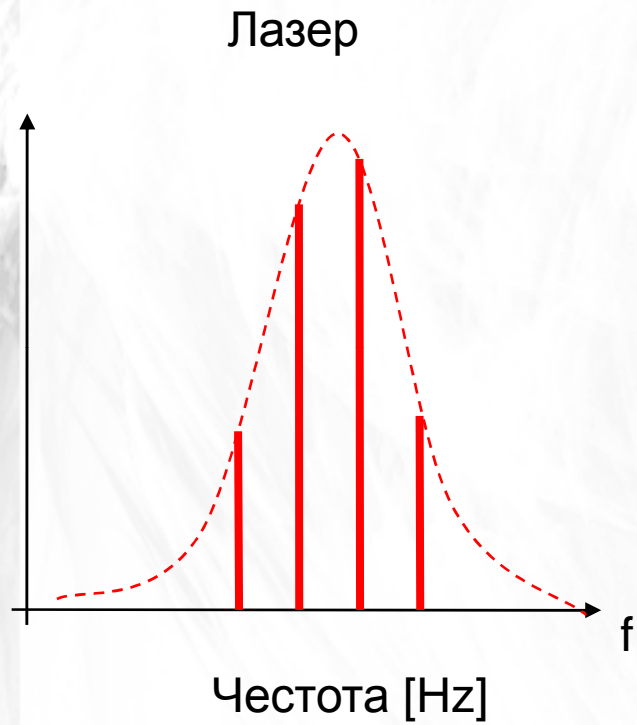


Различна скорост на модовете



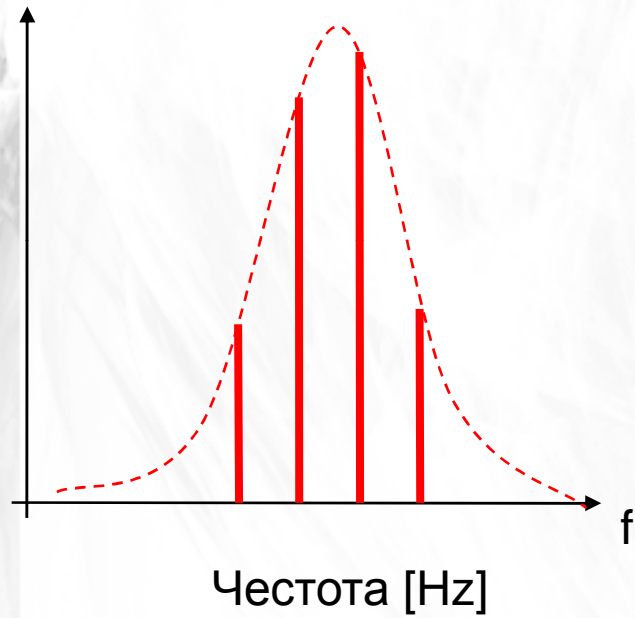
Различна честота на модовете

# Лазер без синхронизация на модовете

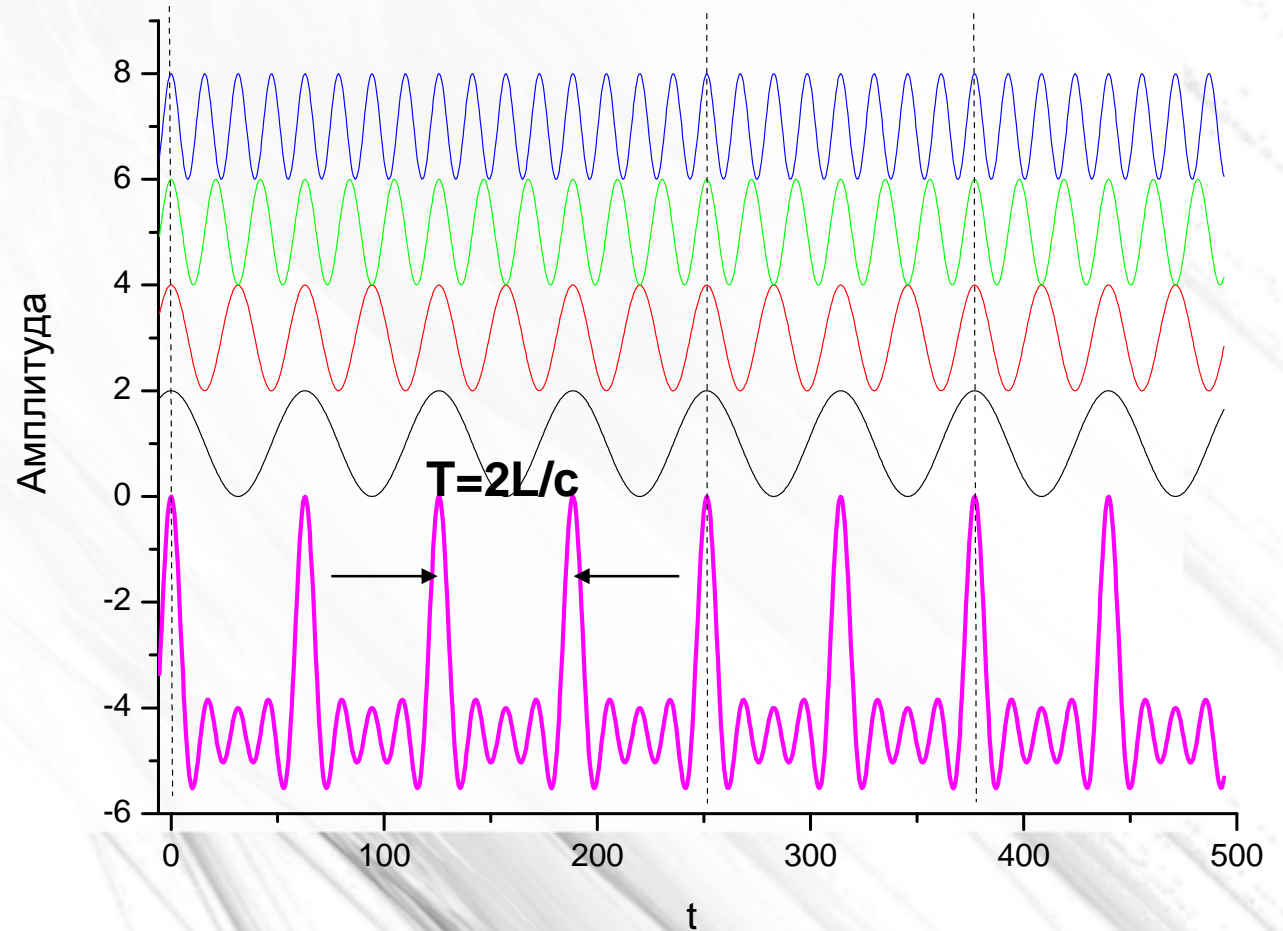


# Лазер със синхронизация на модовете

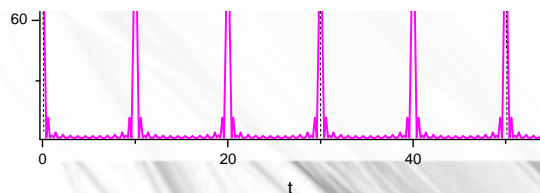
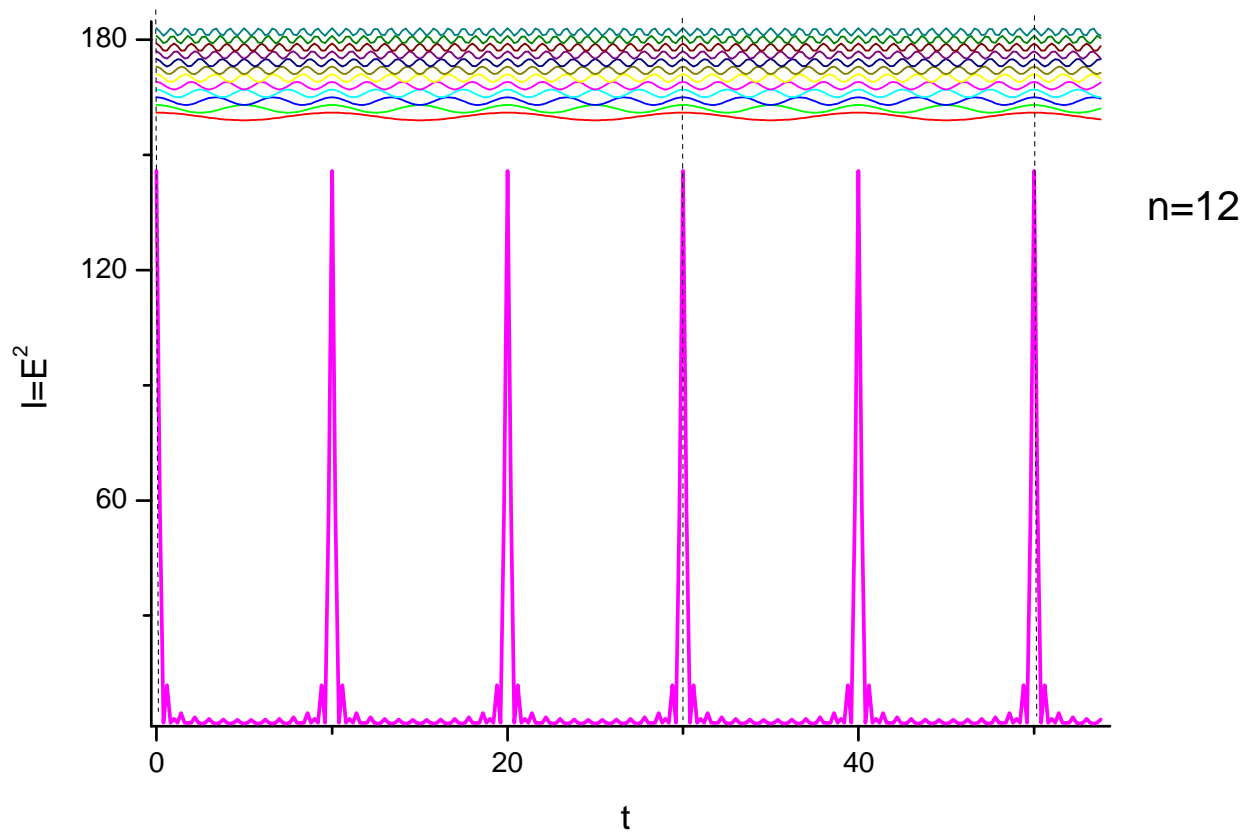
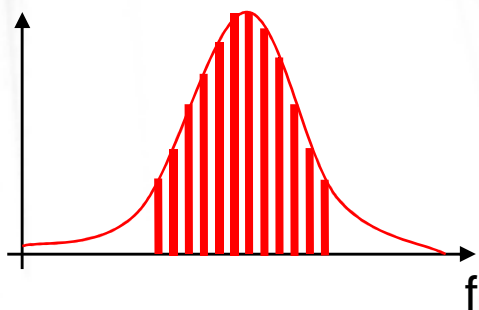
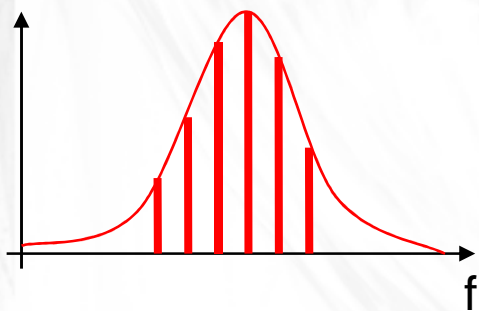
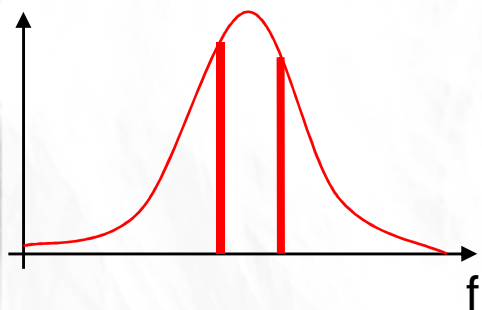
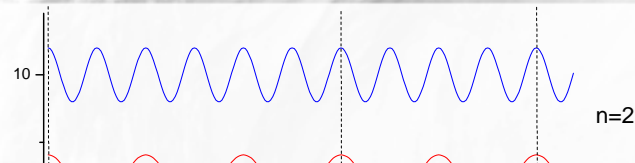
Лазер



Поредица от импулси!

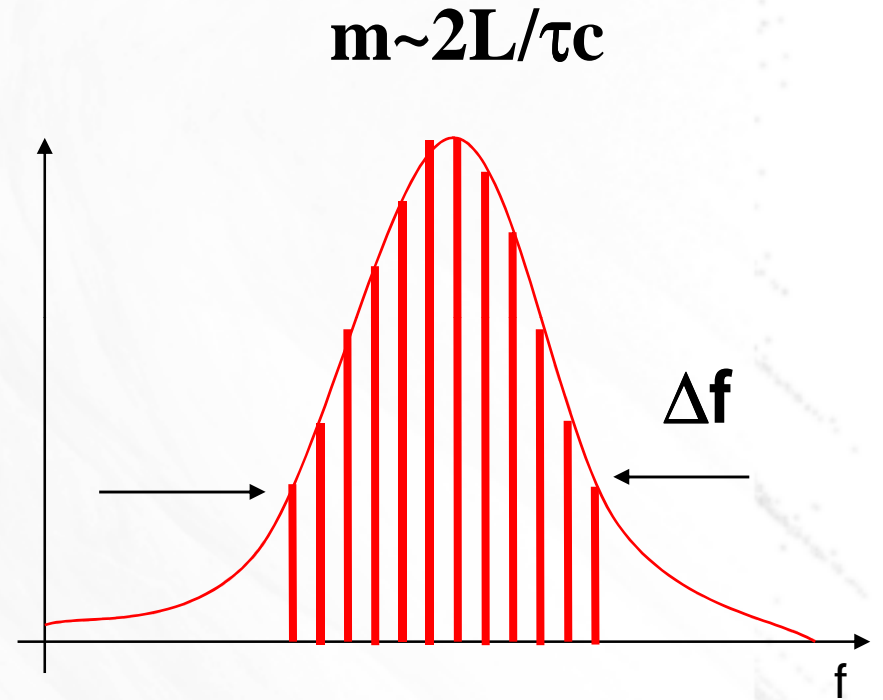
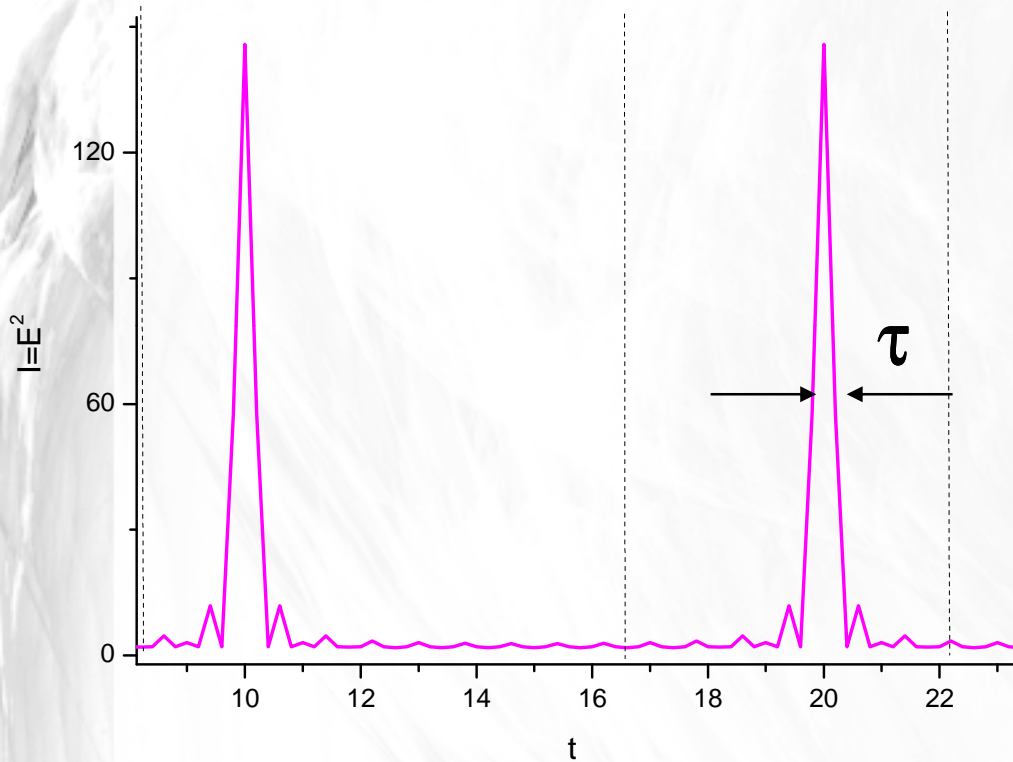


# Колко е ширината на един импулс?



**1 fs =  $10^{-15}$  s**

$\tau \sim 1/\Delta f$



**$\tau = 10$  fs,  $\Delta f = 10^{14}$  Hz       $\lambda_0 = 800$  nm       $\Delta \lambda = 200$  nm**

He-Ne:  $\Delta f = 1,5 \cdot 10^9$  Hz      Ti:Sapphire:  $\Delta f = 1,3 \cdot 10^{14}$  Hz

Диоден лазер:  $\Delta f = 10^{12}$  Hz

**$L = 1$  m,  $\tau = 100$  fs       $m = 67\ 000$  мода**

# Методи за синхронизация на модовете

